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Exercise 1

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Exercise 1 a)

Describe the Cheung formula.

Compute the Cheung formula for the values  $N = 1000, m = 100, k = 15$

Solution

Read the paragraph on *Selecting  $k$  non-distinct items* in the chapter *Counting the Number of Direct Accesses* in the script .

To compute the result, plug in the values in the formula.

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Exercise 2

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Exercise 2 a)

Read the chapter on *Genetic Algorithms* in the *Probabilistic Algorithms* section in the script.

Exercise 2 b)

Implement the genetic algorithm for the join ordering problem. It is sufficient to consider only left deep trees.

Note, on a high level, it is easy to implement the algorithm. However you will need a significant number of helper functions.

Feel free to take the solution code and only implement the high level level algorithm (`Run` function).

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Exercise 3

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Queries with multiple predicates may require the evaluation of multiple indices. In what order should you process the predicates?

Solution

- Order predicates by selectivity. Problem: Ignores predicate evaluation cost.

- Better: Order by  $(1 - s)/c$ , where  $s$  is selectivity and  $c$  is evaluation cost of a predicate.
- The above is optimal if the predicates are independent.

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#### Exercise 4

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Instead of using B-Tree one can also use hashing based data structures. For instance, one can build on the idea of extendible hashing

[https://en.wikipedia.org/wiki/Extendible\\_hashing](https://en.wikipedia.org/wiki/Extendible_hashing)

For queries with what type of predicates can you apply such data structures?

Solution

- Only point queries (e.g.:  $R.a = 5$ )
- In principle, can be used for hash joins on base relations.

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#### Exercise 5

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You are given a relation with 6 tuples. These tuples are equally distributed over 3 pages. Compute the average number of page accesses for reading 2 tuples. Assume that all tuples have the same probability to be read.

Solution

**Yao**

Yao assumptions:  $m$  buckets with  $n$  items each. Randomly select  $k$  distinct items.

Yao gives us the average number of qualifying buckets.

Buckets correspond to pages and items to tuples.

Plug in the above values and obtain  $\bar{Y} = 1.8$ .

**Detailed Explanation, no Yao**

There are 2 tuples per page. Think of an urn model with 2 blue, 2 red and 2 green balls. Each colour refers to a page. We want to draw 2 balls at once. This is equivalent to drawing two balls sequentially without replacement. We draw the first ball and it has *some* colour. Then, there are 5 balls left. The probability that the second ball has the same colour is  $1/5$ . Hence, the probability that the second ball has a different colour is  $4/5$ .

Only when we draw the same colour twice we have one page access. Otherwise we have two page accesses. It follows that the average number of page accesses is

$$\frac{1}{5}1 + \frac{4}{5}2 = 1.8.$$

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## Exercise 6

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### *BONUS*

Write a program that allows you to measure some physical properties of your disk.

### Solution

Code: SimpleBenchmark.java

- OS: openSuSe 12.2
- Sequential write: 10.6 MB/s (1.5 ms/page)
- Sequential read: 31.0 MB/s (0.5 ms/page)
- Random write: 2.1 MB/s (7.4 ms/page)
- Random read: 2.3 MB/s (6.7 ms/page)