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Exercise 1

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Given the following schema:

$R_1(a, c, d, e)$

$R_2(a, b)$

$R_3(b, c)$

$R_4(d)$

$R_5(e)$

Determine and classify the query graph induced by each of the following queries. If we don't consider cross products, then how big is the search space for left-deep join trees and busy join trees? Are there deterministic algorithms that find the optimal join order in this query graph's search space in polynomial time?

Exercise 1 a)

```
SELECT DISTINCT *
FROM R1, R2, R3, R4
WHERE R1.c = R3.c
      AND R2.b = R3.b
      AND R1.d = R4.d;
```

Exercise 1 b)

```
SELECT DISTINCT *
FROM R1, R2, R3, R5
WHERE R1.a = R2.a
      AND R1.c = R3.c
      AND R1.e = R5.e
      AND R2.b = R3.b;
```

Exercise 1 c)

```
SELECT DISTINCT *
FROM R1, R2, R3, R5
WHERE R1.a = R2.a
```

AND R1.c = R3.c  
AND R1.d = R4.d  
AND R1.e = R5.e;

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## Exercise 2

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### Exercise 2 a)

Implement G00. You may use the `QueryGraph` and `Tree` classes provided in the solution code.

### Exercise 2 b)

In *Introduction to the Design & Analysis of Algorithms* the author Anany Levitin describes a greedy algorithm to compute Huffman encodings. Read chapter 9.4 Huffman Trees and Codes. Observe the similarity between the described algorithm and G00. Adjust of your G00 implementation so that it can create Huffman trees for appropriate inputs. Note that it is easy to deduce the corresponding Huffman encoding from a Huffman tree.

Try to read it up in the book.

If you have no access to the book, you'll find a description at

[https://en.wikipedia.org/wiki/Huffman\\_coding#Compression](https://en.wikipedia.org/wiki/Huffman_coding#Compression)

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## Exercise 3

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For relation  $R_1$  and  $R_2$  you are given their cardinality  $|R_i|$ , the number of distinct values in an attribute  $A$ , denoted by  $d(R_i.A)$ , the minimum and maximum value  $\min(R_i.A)$  and  $\max(R_i.A)$ , and key/ foreign-key information.

Note: You will find the answers, as given in the solution, in the paper:

<https://www2.cs.duke.edu/courses/compsci516/cps216/spring03/papers/selinger-etal-1979.pdf>

This paper is the first published article on (cost-based) query optimization!

### Exercise 3 a)

How could you estimate the selectivity of the predicate  $\sigma_{R_1.A=c}$ , where  $c$  is a constant value? Under what assumptions is your estimate accurate?

### Exercise 3 b)

How could you estimate the selectivity of the predicate  $\sigma_{R_1.A>c}$ , where  $c$  is a constant value? Under what assumptions is your estimate accurate?

### Exercise 3 c)

How could you estimate the selectivity of the join predicate  $R_1.A = R_2.B$ ? Under what assumptions is your estimate accurate?

Exercise 3 d)

How could you estimate the selectivity of the conjunctive predicate  $p_1 \wedge p_2$ ? Under what assumptions is your estimate accurate?