CHAIR OF APPLIED COMPUTER SCIENCE III

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Database Systems II Spring Semester 2019 Exercise Sheet 1

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Exercise 1

If you haven't done so already, install a C++ compiler on your computer. If in doubt how to do this, this webpage may be helpful to you:

www.cs.odu.edu/~zeil/cs250PreTest/latest/Public/installingACompiler/

Exercise 2

For each of the following functions, give the asymptotic runtime in "Big O" notation. All examples are taken from McDowell: *Cracking the Coding Interview: 189 Programming Questions and Solutions.* 6th ed. Palo Alto, CA, 2016.

Exercise 2 a)

```
void printUnorderedPairs (const std::vector<double>& V) {
  for (unsigned i = 0; i < V.size(); ++i) {
    for (unsigned j = i+1; j < V.size(); ++j) {
      std::cout << "{" << V[i] << "," << V[j] << "}" << std::endl;
    }
  }
}
</pre>
```

Exercise 2 b)

```
1 int factorial (int n) {
    if (n < 0) {
                                    // case (i)
2
     return -1;
3
    else if (n == 0) \{
                                    // case (ii)
4
     return 1;
5
                                    // case (iii)
   else \{
6
     return n * factorial (n-1);
    }
8
9 }
```

Exercise 2 c)

void allFib (int n) {

```
for (int i = 0; i <= n; ++i) {
2
      std::cout << "fib(" << i << "): " << fib(i) << std::endl;
3
    }
4
5 }
6
7 int fib (int n) {
    if (n == 0 || n == 1) {
8
      return n;
9
    }
10
    return fib(n-1) + fib(n-2);
11
12 }
```

Exercise 3

Exercise 3 a)

Implement a function that finds all positive integer solutions to the equation

$$a^2 + b^2 = c^2 + d^2$$

where $a, b, c, d \in [0, 1000]$. Try to find an efficient solution. What is the asymptotic runtime of your function?

Optional: Measure the actual runtime of your function.

Exercise 3 b)

Implement a function that compresses a string using counts of repeated characters¹. For example, the string aabcccccaaa becomes a2bc5a3. Note that if a character occurs only once, then its count is not part of the compressed string.

Exercise 3 c)

Implement a stack class, i.e., a LIFO container. Your class is expected to provide the following function members:

- pop(): Remove the top item from the stack
- push(item): Add an item to the top of the stack
- top(): Return the top of the stack
- isEmpty(): Return true if and only if the stack is empty

Exercise 4

In the source code provided on the website you'll find a simple binary tree class, cf.

¹Run-length encoding, see https://en.wikipedia.org/wiki/Run-length_encoding

binaryTree.hh and binaryTree.cc. In addition you'll find a file main.cc with a main function and several stubs of functions to be implemented.

On unix systems, you can use of the makefile to compile your code by simply typing make in the command line. Otherwise manually call the compiler with all source files (.cc ending) as input.

Exercise 4 a)

Implement the copy constructor of the class Node such that if performs a deep copy of its subtree. In addition, write COPY to the standard output.

Implement the destructor of the class Node such that, upon destruction of a Node, all child nodes are destructed and their memory is freed.

Note: Follow this link for information on copy-constructors, destructors and pointers: http://www.cplusplus.com/doc/tutorial/classes2/

Exercise 4 b)

Implement the print function of the class Node to output a tree in in-order ordering such that the value of a node and the values of its children are surrounded by brackets. See the following example for an illustration: The tree:

The output: ((3)1(4))0((5)2(6))

Exercise 4 c)

Implement two functions foo and bar. Both take as parameter the root node of a tree. However, foo calls the root node by value whereas bar calls the root node by reference. Note: Follow this link for information on call-by-value and call-by-reference: http://www.cplusplus.com/articles/z6vU7k9E/

Exercise 4 d)

Implement a function isSymmetric that returns true if and only if the tree is axial symmetric around a vertical axis through the root node. For instance, for this tree, isSymmetric must return true:

0 / \ $\begin{array}{ccc}1&1\\/&/\\3&4&4&3\end{array}$

Exercise 4 e)

Implement a function **invert** that inverts a given tree. See the following example for an illustration:

The tree:



Inverted tree:





Implement a function flatten that transforms a given tree to a linked-list by reassigning the node's child pointers. Try to perform this transformation in-place, meaning that no new memory must be allocated except for auxiliary variables. See the following example for an illustration: The tree:

Tree as linked-list:

0-1-3-4-2-5-6