

HIMMELBLAU

Mk function: @(x)hessf(x)

x0 = [5.00 ; 5.00]

.. #	0: R=	NaN	f(x)=	890	x(1)=	5	x(2)=	5	step=	NaN	crate=	NaN	gradf	=	655.35
NF # 1:	R=	0.71831	f(x)=	114.81	x(1)=	3.6856	x(2)=	3.4849	step=	1	crate=	NaN	gradf	=	172.52
NF # 2:	R=	0.64708	f(x)=	9.4933	x(1)=	3.0779	x(2)=	2.609	step=	1	crate=	NaN	gradf	=	37.497
NF # 3:	R=	0.46067	f(x)=	0.46668	x(1)=	2.9665	x(2)=	2.1716	step=	1	crate=	0.4233	gradf	=	5.9624
NF # 4:	R=	0.30708	f(x)=	0.0053798	x(1)=	2.9956	x(2)=	2.0193	step=	1	crate=	0.34376	gradf	=	0.57799
NF # 5:	R=	0.24684	f(x)=	1.1589e-06	x(1)=	2.9999	x(2)=	2.0003	step=	1	crate=	0.12551	gradf	=	0.0084733
NF # 6:	R=	0.23958	f(x)=	5.7423e-14	x(1)=	3	x(2)=	2	step=	1	crate=	0.014914	gradf	=	1.8826e-06
NF # 7:	R=	0.23947	f(x)=	1.5777e-28	x(1)=	3	x(2)=	2	step=	1	crate=	0.0002281	gradf	=	1.1291e-13

Mk function: @(x)hessf(x)

Hessian approximation at last iterate (rank = 2, condition = 3.199764e+00, eigenvalues = (25.7157, 82.2843)):

74	20
20	34.000000000001

Hessian (exact) at last iterate (rank = 2, condition = 3.199764e+00, eigenvalues = (25.7157, 82.2843)):

74	20
20	34.000000000001

x0 = [5.00 ; 5.00]
x = [3.00000000 ; 2.00000000]
f(x) = 1.5777218e-28
#it = 7 #f = 22 #gradf = 8 #hessf = 7

Mk function: @(x)diag(diag(hessf(x)))

x0 = [5.00 ; 5.00]

.. #	0: R=	NaN	f(x)=	890	x(1)=	5	x(2)=	5	step=	NaN	crate=	NaN	gradf	=	655.35
NF # 1:	R=	0.94558	f(x)=	73.485	x(1)=	3.4676	x(2)=	3.3061	step=	1	crate=	NaN	gradf	=	130.18
NF # 2:	R=	0.97044	f(x)=	3.0801	x(1)=	2.8196	x(2)=	2.4115	step=	1	crate=	NaN	gradf	=	15.015
NF # 3:	R=	0.87335	f(x)=	0.54529	x(1)=	2.8819	x(2)=	2.1483	step=	1	crate=	0.24484	gradf	=	6.1814
NF # 4:	R=	0.6174	f(x)=	0.086525	x(1)=	2.962	x(2)=	2.0706	step=	1	crate=	0.41236	gradf	=	2.2132
NF # 5:	R=	0.52117	f(x)=	0.014009	x(1)=	2.9809	x(2)=	2.0236	step=	1	crate=	0.45392	gradf	=	1.0271
NF # 6:	R=	0.48216	f(x)=	0.0022249	x(1)=	2.9937	x(2)=	2.0113	step=	1	crate=	0.35117	gradf	=	0.35453
NF # 7:	R=	0.46905	f(x)=	0.00035471	x(1)=	2.997	x(2)=	2.0038	step=	1	crate=	0.46185	gradf	=	0.16454
NF # 8:	R=	0.46301	f(x)=	5.6382e-05	x(1)=	2.999	x(2)=	2.0018	step=	1	crate=	0.34409	gradf	=	0.056478
NF # 9:	R=	0.46098	f(x)=	8.9677e-06	x(1)=	2.9995	x(2)=	2.0006	step=	1	crate=	0.46335	gradf	=	0.02619
NF # 10:	R=	0.46002	f(x)=	1.4257e-06	x(1)=	2.9998	x(2)=	2.0003	step=	1	crate=	0.34309	gradf	=	0.0089821
NF # 11:	R=	0.4597	f(x)=	2.2667e-07	x(1)=	2.9999	x(2)=	2.0001	step=	1	crate=	0.4636	gradf	=	0.0041646
NF # 12:	R=	0.45955	f(x)=	3.6037e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.34293	gradf	=	0.0014281
NF # 13:	R=	0.4595	f(x)=	5.7293e-09	x(1)=	3	x(2)=	2	step=	1	crate=	0.46363	gradf	=	0.00066212
NF # 14:	R=	0.45947	f(x)=	9.1085e-10	x(1)=	3	x(2)=	2	step=	1	crate=	0.3429	gradf	=	0.00022704
NF # 15:	R=	0.45947	f(x)=	1.4481e-10	x(1)=	3	x(2)=	2	step=	1	crate=	0.46364	gradf	=	0.00010527
NF # 16:	R=	0.45946	f(x)=	2.3022e-11	x(1)=	3	x(2)=	2	step=	1	crate=	0.3429	gradf	=	3.6096e-05
NF # 17:	R=	0.45946	f(x)=	3.6601e-12	x(1)=	3	x(2)=	2	step=	1	crate=	0.46364	gradf	=	1.6735e-05
NF # 18:	R=	0.45946	f(x)=	5.819e-13	x(1)=	3	x(2)=	2	step=	1	crate=	0.3429	gradf	=	5.7386e-06
NF # 19:	R=	0.45946	f(x)=	9.2511e-14	x(1)=	3	x(2)=	2	step=	1	crate=	0.46364	gradf	=	2.6606e-06
NF # 20:	R=	0.45946	f(x)=	1.4708e-14	x(1)=	3	x(2)=	2	step=	1	crate=	0.3429	gradf	=	9.1233e-07

Mk function: @(x)diag(diag(hessf(x)))

Hessian approximation at last iterate (rank = 2, condition = 2.176470e+00, eigenvalues = (34, 74)):

73.999989369146	0
0	34.0000013255468

Hessian (exact) at last iterate (rank = 2, condition = 3.199764e+00, eigenvalues = (25.7157, 82.2843)):

73.999989369146	20.0000000504203
20.0000000504203	34.0000013255468

x0 = [5.00 ; 5.00]
x = [2.99999998 ; 2.00000003]
f(x) = 1.4707689e-14
#it = 20 #f = 61 #gradf = 21 #hessf = 20

Mk function: @(x)hessf(x0)

x0 = [5.00 ; 5.00]

.. #	0: R=	NaN	f(x)=	890	x(1)=	5	x(2)=	5	step=	NaN	crate=	NaN	gradf	=	655.35
NF # 1:	R=	0.71831	f(x)=	114.81	x(1)=	3.6856	x(2)=	3.4849	step=	1	crate=	NaN	gradf	=	172.52
NF # 2:	R=	0.71831	f(x)=	44.699	x(1)=	3.3601	x(2)=	3.0693	step=	1	crate=	NaN	gradf	=	96.184
NF # 3:	R=	0.71831	f(x)=	21.582	x(1)=	3.1908	x(2)=	2.8281	step=	1	crate=	0.55813	gradf	=	61.64
NF # 4:	R=	0.71831	f(x)=	11.759	x(1)=	3.0916	x(2)=	2.6667	step=	1	crate=	0.64265	gradf	=	42.488
NF # 5:	R=	0.71831	f(x)=	6.9714	x(1)=	3.0308	x(2)=	2.5504	step=	1	crate=	0.69282	gradf	=	30.715
NF # 6:	R=	0.71831	f(x)=	4.4105	x(1)=	2.9931	x(2)=	2.4626	step=	1	crate=	0.72872	gradf	=	23.01
NF # 7:	R=	0.71831	f(x)=	2.9393	x(1)=	2.97	x(2)=	2.3939	step=	1	crate=	0.75754	gradf	=	17.747
NF # 8:	R=	0.71831	f(x)=	2.0427	x(1)=	2.9565	x(2)=	2.3389	step=	1	crate=	0.78224	gradf	=	14.034
NF # 9:	R=	0.71831	f(x)=	1.4676	x(1)=	2.9493	x(2)=	2.2939	step=	1	crate=	0.80387	gradf	=	11.343
NF # 10:	R=	0.71831	f(x)=	1.0823	x(1)=	2.9463	x(2)=	2.2566	step=	1	crate=	0.82264	gradf	=	9.3444
NF # 11:	R=	0.71831	f(x)=	0.81444	x(1)=	2.946	x(2)=	2.2252	step=	1	crate=	0.83851	gradf	=	7.8238
NF # 12:	R=	0.71831	f(x)=	0.6224	x(1)=	2.9475	x(2)=	2.1984	step=	1	crate=	0.85149	gradf	=	6.6404
NF # 13:	R=	0.71831	f(x)=	0.48129	x(1)=	2.95	x(2)=	2.1755	step=	1	crate=	0.86179	gradf	=	5.6993
NF # 14:	R=	0.71831	f(x)=	0.37555	x(1)=	2.9531	x(2)=	2.1557	step=	1	crate=	0.86976	gradf	=	4.9357
NF # 15:	R=	0.71831	f(x)=	0.29509	x(1)=	2.9565	x(2)=	2.1385	step=	1	crate=	0.87585	gradf	=	4.3053
NF # 16:	R=	0.71831	f(x)=	0.23314	x(1)=	2.96	x(2)=	2.1234	step=	1	crate=	0.88047	gradf	=	3.777
NF # 17:	R=	0.71831	f(x)=	0.18501	x(1)=	2.9634	x(2)=	2.1102	step=	1	crate=	0.88399	gradf	=	3.3287
NF # 18:	R=	0.71831	f(x)=	0.14733	x(1)=	2.9667	x(2)=	2.0985	step=	1	crate=	0.88669	gradf	=	2.9443
NF # 19:	R=	0.71831	f(x)=	0.11766	x(1)=	2.9698	x(2)=	2.0882	step=	1	crate=	0.88882	gradf	=	2.612
NF # 20:	R=	0.71831	f(x)=	0.094204	x(1)=	2.9727	x(2)=	2.0791	step=	1	crate=	0.89052	gradf	=	2.3229
NF # 21:	R=	0.71831	f(x)=	0.075579	x(1)=	2.9753	x(2)=	2.0709	step=	1	crate=	0.89191	gradf	=	2.0699
NF # 22:	R=	0.71831	f(x)=	0.060745	x(1)=	2.9777	x(2)=	2.0637	step=	1	crate=	0.89309	gradf	=	1.8476
NF # 23:	R=	0.71831	f(x)=	0.048899	x(1)=	2.9799	x(2)=	2.0572	step=	1	crate=	0.89409	gradf	=	1.6514
NF # 24:	R=	0.71831	f(x)=	0.039417	x(1)=	2.9819	x(2)=	2.0514	step=	1	crate=	0.89497	gradf	=	1.4779
NF # 25:	R=	0.71831	f(x)=	0.031813	x(1)=	2.9837	x(2)=	2.0463	step=	1	crate=	0.89574	gradf	=	1.3241
NF # 26:	R=	0.71831	f(x)=	0.025703	x(1)=	2.9854	x(2)=	2.0416	step=	1	crate=	0.89644	gradf	=	1.1873
NF # 27:	R=	0.71831	f(x)=	0.020786	x(1)=	2.9868	x(2)=	2.0375	step=	1	crate=	0.89706	gradf	=	1.0655
NF # 28:	R=	0.71831	f(x)=	0.016825	x(1)=	2.9882	x(2)=	2.0337	step=	1	crate=	0.89763	gradf	=	0.95681
NF # 29:	R=	0.71831	f(x)=	0.013629	x(1)=	2.9893	x(2)=	2.0304	step=	1	crate=	0.89814	gradf	=	0.85976

NF # 30: R=	0.71831	f(x)=	0.011047	x(1)=	2.9904	x(2)=	2.0274	step=	1	crate=	0.8986	gradf =	0.77298
NF # 31: R=	0.71831	f(x)=	0.0089606	x(1)=	2.9914	x(2)=	2.0247	step=	1	crate=	0.89903	gradf =	0.69528
NF # 32: R=	0.71831	f(x)=	0.007272	x(1)=	2.9922	x(2)=	2.0223	step=	1	crate=	0.89941	gradf =	0.62566
NF # 33: R=	0.71831	f(x)=	0.0059045	x(1)=	2.993	x(2)=	2.0201	step=	1	crate=	0.89976	gradf =	0.56323
NF # 34: R=	0.71831	f(x)=	0.0047964	x(1)=	2.9937	x(2)=	2.0181	step=	1	crate=	0.90008	gradf =	0.50719
NF # 35: R=	0.71831	f(x)=	0.0038978	x(1)=	2.9943	x(2)=	2.0163	step=	1	crate=	0.90037	gradf =	0.45686
NF # 36: R=	0.71831	f(x)=	0.0031687	x(1)=	2.9949	x(2)=	2.0147	step=	1	crate=	0.90063	gradf =	0.41164
NF # 37: R=	0.71831	f(x)=	0.0025768	x(1)=	2.9954	x(2)=	2.0133	step=	1	crate=	0.90087	gradf =	0.37099
NF # 38: R=	0.71831	f(x)=	0.0020961	x(1)=	2.9958	x(2)=	2.012	step=	1	crate=	0.90109	gradf =	0.33442
NF # 39: R=	0.71831	f(x)=	0.0017055	x(1)=	2.9963	x(2)=	2.0108	step=	1	crate=	0.90128	gradf =	0.30151
NF # 40: R=	0.71831	f(x)=	0.0013881	x(1)=	2.9966	x(2)=	2.0098	step=	1	crate=	0.90146	gradf =	0.27188
NF # 41: R=	0.71831	f(x)=	0.00113	x(1)=	2.997	x(2)=	2.0088	step=	1	crate=	0.90162	gradf =	0.24521
NF # 42: R=	0.71831	f(x)=	0.00092001	x(1)=	2.9973	x(2)=	2.0079	step=	1	crate=	0.90177	gradf =	0.22118
NF # 43: R=	0.71831	f(x)=	0.00074921	x(1)=	2.9975	x(2)=	2.0072	step=	1	crate=	0.9019	gradf =	0.19953
NF # 44: R=	0.71831	f(x)=	0.00061021	x(1)=	2.9978	x(2)=	2.0065	step=	1	crate=	0.90202	gradf =	0.18003
NF # 45: R=	0.71831	f(x)=	0.00049707	x(1)=	2.998	x(2)=	2.0058	step=	1	crate=	0.90213	gradf =	0.16244
NF # 46: R=	0.71831	f(x)=	0.00040496	x(1)=	2.9982	x(2)=	2.0053	step=	1	crate=	0.90223	gradf =	0.14659
NF # 47: R=	0.71831	f(x)=	0.00032995	x(1)=	2.9984	x(2)=	2.0048	step=	1	crate=	0.90231	gradf =	0.13229
NF # 48: R=	0.71831	f(x)=	0.00026887	x(1)=	2.9985	x(2)=	2.0043	step=	1	crate=	0.90239	gradf =	0.1194
NF # 49: R=	0.71831	f(x)=	0.00021912	x(1)=	2.9987	x(2)=	2.0039	step=	1	crate=	0.90247	gradf =	0.10777
NF # 50: R=	0.71831	f(x)=	0.00017858	x(1)=	2.9988	x(2)=	2.0035	step=	1	crate=	0.90253	gradf =	0.097275
NF # 51: R=	0.71831	f(x)=	0.00014556	x(1)=	2.9989	x(2)=	2.0032	step=	1	crate=	0.90259	gradf =	0.08781
NF # 52: R=	0.71831	f(x)=	0.00011865	x(1)=	2.999	x(2)=	2.0029	step=	1	crate=	0.90264	gradf =	0.079269
NF # 53: R=	0.71831	f(x)=	9.6725e-05	x(1)=	2.9991	x(2)=	2.0026	step=	1	crate=	0.90269	gradf =	0.071563
NF # 54: R=	0.71831	f(x)=	7.8854e-05	x(1)=	2.9992	x(2)=	2.0023	step=	1	crate=	0.90274	gradf =	0.064608
NF # 55: R=	0.71831	f(x)=	6.4288e-05	x(1)=	2.9993	x(2)=	2.0021	step=	1	crate=	0.90278	gradf =	0.058331
NF # 56: R=	0.71831	f(x)=	5.2415e-05	x(1)=	2.9993	x(2)=	2.0019	step=	1	crate=	0.90281	gradf =	0.052666
NF # 57: R=	0.71831	f(x)=	4.2736e-05	x(1)=	2.9994	x(2)=	2.0017	step=	1	crate=	0.90284	gradf =	0.047552
NF # 58: R=	0.71831	f(x)=	3.4847e-05	x(1)=	2.9995	x(2)=	2.0015	step=	1	crate=	0.90287	gradf =	0.042936
NF # 59: R=	0.71831	f(x)=	2.8414e-05	x(1)=	2.9995	x(2)=	2.0014	step=	1	crate=	0.9029	gradf =	0.038769
NF # 60: R=	0.71831	f(x)=	2.317e-05	x(1)=	2.9996	x(2)=	2.0013	step=	1	crate=	0.90292	gradf =	0.035007
NF # 61: R=	0.71831	f(x)=	1.8894e-05	x(1)=	2.9996	x(2)=	2.0011	step=	1	crate=	0.90294	gradf =	0.031611
NF # 62: R=	0.71831	f(x)=	1.5408e-05	x(1)=	2.9996	x(2)=	2.001	step=	1	crate=	0.90296	gradf =	0.028544
NF # 63: R=	0.71831	f(x)=	1.2565e-05	x(1)=	2.9997	x(2)=	2.0009	step=	1	crate=	0.90298	gradf =	0.025776
NF # 64: R=	0.71831	f(x)=	1.0247e-05	x(1)=	2.9997	x(2)=	2.0008	step=	1	crate=	0.903	gradf =	0.023276
NF # 65: R=	0.71831	f(x)=	8.3566e-06	x(1)=	2.9997	x(2)=	2.0008	step=	1	crate=	0.90301	gradf =	0.021019
NF # 66: R=	0.71831	f(x)=	6.8151e-06	x(1)=	2.9998	x(2)=	2.0007	step=	1	crate=	0.90302	gradf =	0.018982
NF # 67: R=	0.71831	f(x)=	5.5581e-06	x(1)=	2.9998	x(2)=	2.0006	step=	1	crate=	0.90304	gradf =	0.017141
NF # 68: R=	0.71831	f(x)=	4.533e-06	x(1)=	2.9998	x(2)=	2.0006	step=	1	crate=	0.90305	gradf =	0.01548
NF # 69: R=	0.71831	f(x)=	3.697e-06	x(1)=	2.9998	x(2)=	2.0005	step=	1	crate=	0.90305	gradf =	0.013979
NF # 70: R=	0.71831	f(x)=	3.0152e-06	x(1)=	2.9998	x(2)=	2.0005	step=	1	crate=	0.90306	gradf =	0.012624
NF # 71: R=	0.71831	f(x)=	2.4592e-06	x(1)=	2.9999	x(2)=	2.0004	step=	1	crate=	0.90307	gradf =	0.011401
NF # 72: R=	0.71831	f(x)=	2.0057e-06	x(1)=	2.9999	x(2)=	2.0004	step=	1	crate=	0.90308	gradf =	0.010296
NF # 73: R=	0.71831	f(x)=	1.6359e-06	x(1)=	2.9999	x(2)=	2.0003	step=	1	crate=	0.90308	gradf =	0.0092984
NF # 74: R=	0.71831	f(x)=	1.3342e-06	x(1)=	2.9999	x(2)=	2.0003	step=	1	crate=	0.90309	gradf =	0.0083974
NF # 75: R=	0.71831	f(x)=	1.0882e-06	x(1)=	2.9999	x(2)=	2.0003	step=	1	crate=	0.9031	gradf =	0.0075837
NF # 76: R=	0.71831	f(x)=	8.8757e-07	x(1)=	2.9999	x(2)=	2.0002	step=	1	crate=	0.9031	gradf =	0.0068489
NF # 77: R=	0.71831	f(x)=	7.2393e-07	x(1)=	2.9999	x(2)=	2.0002	step=	1	crate=	0.9031	gradf =	0.0061853
NF # 78: R=	0.71831	f(x)=	5.9046e-07	x(1)=	2.9999	x(2)=	2.0002	step=	1	crate=	0.90311	gradf =	0.0055861
NF # 79: R=	0.71831	f(x)=	4.816e-07	x(1)=	2.9999	x(2)=	2.0002	step=	1	crate=	0.90311	gradf =	0.0050449
NF # 80: R=	0.71831	f(x)=	3.9281e-07	x(1)=	2.9999	x(2)=	2.0002	step=	1	crate=	0.90311	gradf =	0.0045561
NF # 81: R=	0.71831	f(x)=	3.2039e-07	x(1)=	2.9999	x(2)=	2.0001	step=	1	crate=	0.90312	gradf =	0.0041147
NF # 82: R=	0.71831	f(x)=	2.6132e-07	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90312	gradf =	0.0037161
NF # 83: R=	0.71831	f(x)=	2.1315e-07	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90312	gradf =	0.0033561
NF # 84: R=	0.71831	f(x)=	1.7385e-07	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90312	gradf =	0.003031
NF # 85: R=	0.71831	f(x)=	1.418e-07	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0027374
NF # 86: R=	0.71831	f(x)=	1.1566e-07	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0024722
NF # 87: R=	0.71831	f(x)=	9.434e-08	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0022327
NF # 88: R=	0.71831	f(x)=	7.6949e-08	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0020165
NF # 89: R=	0.71831	f(x)=	6.2764e-08	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0018211
NF # 90: R=	0.71831	f(x)=	5.1194e-08	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0016447
NF # 91: R=	0.71831	f(x)=	4.1757e-08	x(1)=	3	x(2)=	2.0001	step=	1	crate=	0.90313	gradf =	0.0014854
NF # 92: R=	0.71831	f(x)=	3.4059e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90313	gradf =	0.0013415
NF # 93: R=	0.71831	f(x)=	2.7781e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.0012116
NF # 94: R=	0.71831	f(x)=	2.266e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.0010942
NF # 95: R=	0.71831	f(x)=	1.8482e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.00098824
NF # 96: R=	0.71831	f(x)=	1.5075e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.00089252
NF # 97: R=	0.71831	f(x)=	1.2296e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.00080607
NF # 98: R=	0.71831	f(x)=	1.003e-08	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.00072799
NF # 99: R=	0.71831	f(x)=	8.1809e-09	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.00065748
NF #100: R=	0.71831	f(x)=	6.6729e-09	x(1)=	3	x(2)=	2	step=	1	crate=	0.90314	gradf =	0.0005938

Mk function: @(x)hessf(x0)

Hessian approximation at last iterate (rank = 2, condition = 1.332715e+00, eigenvalues = (245.208, 326.792)):

278 40
40 294

Hessian (exact) at last iterate (rank = 2, condition = 3.199664e+00, eigenvalues = (25.7165, 82.2841)):

73.9995565485379 20.0000564310929
20.0000564310929 34.0010006324777

x0 = [5.00 ; 5.00]
x = [2.99999265 ; 2.00002146]
f(x) = 6.6728755e-09
#it = 100 #f = 301 #gradf = 101 #hessf = 100

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